

Test Analysis (Mathematics)					
Student Name :			Batch :		
Type	Marking Scheme	Right	Wrong	Left	Score
Single Answer Correct (Q1-Q10)	+4, -1				
Multiple Answer Correct (Q11-Q18)	+4, -1				
Numerical Answer Type (Q19-Q25)	+4, -1				
<b>Total</b>					

**Single Choice Correct Type**

- $x = \sqrt{2 + \sqrt{2 + \sqrt{2 + \dots \infty}}}$  then  $x =$

(A) 2 and -1 (B) 2 and 1  
(C) -1 (D) none of these
- The number of real solutions of the equation  $|x|^2 - 4|x| + 3 = 0$  is

(A) 4 (B) 2  
(C) 1 (D) 3
- If the roots of the quadratic equation  $x^2 - ax + b = 0$  are real and differ by a quantity less than 1, then

(A)  $b > \frac{a^2}{4}$  (B)  $b < \frac{a^2 - 1}{4}$   
(C)  $\frac{a^2 - 1}{4} < b < \frac{a^2}{4}$  (D) none of these
- The set of values of 'a' for which the equation  $x^3 - 3x + a = 0$  has three distinct real roots, is

(A)  $(-\infty, \infty)$  (B)  $(-2, 2)$   
(C)  $(-1, 1)$  (D) none of these
- The least integral value of k such that  $(k-2)x^2 + 8x + k + 4$  is positive for all real values of x is

(A) 1 (B) 2  
(C) 3 (D) 5
- If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 - P(x+1) - q = 0$  then the value of  $\frac{\alpha^2 + 2\alpha + 1}{\alpha^2 + 2\alpha + q} + \frac{\beta^2 + 2\beta + 1}{\beta^2 + 2\beta + q}$  is

(A) 2 (B) 1  
(C) 0 (D) None
- In the quadratic equation  $ax^2 + bx + c = 0$ ,  $\Delta = b^2 - 4ac$  and  $\alpha + \beta$ ,  $\alpha^2 + \beta^2$ ,  $\alpha^3 + \beta^3$ , are in G.P. where  $\alpha, \beta$  are the root of  $ax^2 + bx + c = 0$ , then

(A)  $\Delta \neq 0$  (B)  $b\Delta = 0$   
(C)  $c\Delta = 0$  (D)  $\Delta = 0$
- The sum of real roots of the equation  $x^2 - 2^{2008}x + |x - 2^{2007}| + 2(2^{4013} - 1) = 0$

(A)  $2^{2007}$  (B)  $2^{2006}$   
(C)  $2^{2008}$  (D) None of these

9. If  $x_1$  and  $x_2$  are the roots of  $x^2 + (\sin \theta - 1)x - \frac{1}{2} \cos^2 \theta = 0$  then the maximum value of  $x_1^2 + x_2^2 =$   
 (A) 2 (B) 3  
 (C)  $\frac{9}{4}$  (D) 4
10. If  $f(x) = 0$  is a cubic equation with positive and distinct roots  $\alpha, \beta, \gamma$  such that  $\beta$  is the H.M of the roots of  $f'(x) = 0$ . then  $\alpha, \beta, \gamma$  are in  
 (A) A.P (B) G.P  
 (C) H.P (D) none of these

**Multiple Choice Correct Type**

11. If  $a, b \in \{1, 2, 3, 4\}$  and  $ax^2 + bx + 1 = 0$  has real roots, then  
 (A)  $a > b$  (B)  $a \leq b$   
 (C) Number of possible pairs  $(a, b)$  is 7 (D) none of these
12. The values(s) which 'c' may take so that  $x^3 - 6x^2 + 9x - c$  is of the form  $(x - \alpha)^2(x - \beta)$  ( $\alpha, \beta$  real) is/are  
 (A) 0 (B) 4  
 (C) 1 (D) 3
13. Let  $\alpha, \beta$  be the roots of  $x^2 - 4x + A = 0$  and  $\gamma, \delta$  be the roots of  $x^2 - 36x + B = 0$ . If  $\alpha, \beta, \gamma, \delta$  form an increasing G.P., then  
 (A)  $B = 81A$  (B)  $A = 3$   
 (C)  $B = 243$  (D)  $A + B = 251$
14. If the equation  $cx^2 + bx - 2a = 0$  has no real roots and  $a < \frac{b+c}{2}$  then  
 (A)  $ac < 0$  (B)  $a < 0$   
 (C)  $\frac{c-b}{2} > a$  (D)  $\frac{c+2b}{8} > a$
15. If  $a, b$  and  $c$  are three terms of an A.P such that  $a \neq b$  then  $\frac{b-c}{a-b}$  may be equal to  
 (A)  $\sqrt{2}$  (B)  $\sqrt{3}$   
 (C) 1 (D) 3
16. Let  $a, b, c \in \mathbb{R}$ . If  $ax^2 + bx + c = 0$  has two real roots A and B where,  $A < -1$  and  $B > 1$ , Then  
 (A)  $1 + \frac{|b|}{a} + \frac{c}{a} < 0$  (B)  $1 - \frac{|b|}{a} + \frac{c}{a} < 0$   
 (C)  $|c| < |a|$  (D)  $|c| < |a| - |b|$
17. If  $\alpha, \beta$  are roots of  $ax^2 + bx + c = 0, ac \neq 0$ , then  
 (A)  $\frac{1}{\alpha}, \frac{1}{\beta}$  are the roots of  $cx^2 + bx + a = 0$   
 (B)  $-\alpha, -\beta$  are the roots of  $ax^2 - bx + c = 0$   
 (C)  $\alpha^2, \beta^2$  are the roots of  $a^2x^2 - (b^2 - 2ac)x + c^2 = 0$   
 (D)  $2\alpha, 2\beta$  are the roots of  $ax^2 + 2bx + 4c = 0$
18. If  $\alpha$  is one root of the equation  $4x^2 + 2x - 1 = 0$ , then its other root is given by  
 (A)  $4\alpha^3 - 3\alpha$  (B)  $4\alpha^3 + 3\alpha$   
 (C)  $\alpha - (1/2)$  (D)  $-\alpha - (1/2)$

**Numerical Answer Type**

19. The number of real roots of  $(7 + 4\sqrt{3})^{|x|-8} + (7 - 4\sqrt{3})^{|x|-8} = 14$  is
20. The number of integral solutions of  $\frac{x+2}{x^2+1} > \frac{1}{2}$  is 3
21. The number of solutions of the equation  $[2x] - [x+1] = 2x$  must be equal to (where  $[.]$  denotes the greatest integer function)
22. Let  $P(x) = x^3 - 8x^2 + cx - d$  be a polynomial with real coefficients and with all its roots being distinct positive integers. Then number of possible value of  $c$  is \_\_\_\_\_.
23. If  $x^2 + 2ax + a < 0 \forall x \in (1, 2)$  then the minimum value of  $|5a|$  is
24. If the roots of equation  $ax^2 + bx + c = 0$  ( $a \neq 0$ ) are  $\alpha$  and  $\beta$  and the roots of the equation  $a^5x^2 + ba^2c^2x + c^5 = 0$  are 4 & 8 then the numerical value of  $\alpha\beta$  is
25. Let 'S' be the sum of all the integral values of 'a' for which one root of the equation  $(a-5)x^2 - 2ax + a - 4 = 0$  is smaller than 1 and the other is greater than 2, then  $\frac{S-61}{25}$  is equal to